TWO QUESTIONS (CHEAT SHEET)

MICHAEL JOSWIG

1. What is a sparse matrix?

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2. How good are convex hull algorithms?

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